

# Application of MWPC based muography in geophysics, experiments and planning

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2. Eötvös Loránd University, Faculty of Science, Department of Geophysics and Space Science

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- HUN-REN Wigner Group from Hungary
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- Janossy underground laboratory

## ▶ Conclusion

# Muography

1911: Victor Hess: Cosmic ray

Primarily and secondary particles

1936:C. D. Anderson: muon identification

1970: L.Alvarez: first muography experiment

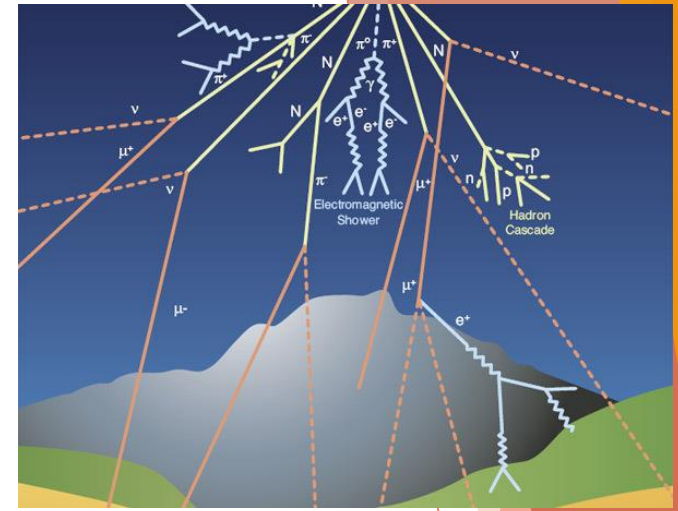
Its characteristics :

- ▶ wide energy spectrum
- ▶ slow energy loss (Bethe-Bloch formula- $\rightarrow \Delta E \sim \rho l$ )
- ▶ The energy loss is proportional to the density of the rock and the trajectory length in the rock

The muonfield:  $F = N / (t \Omega A)$

Muon flux on ground roughly:  $F = F_0 \cos^2 \vartheta$  (100/ sec/m<sup>2</sup>)

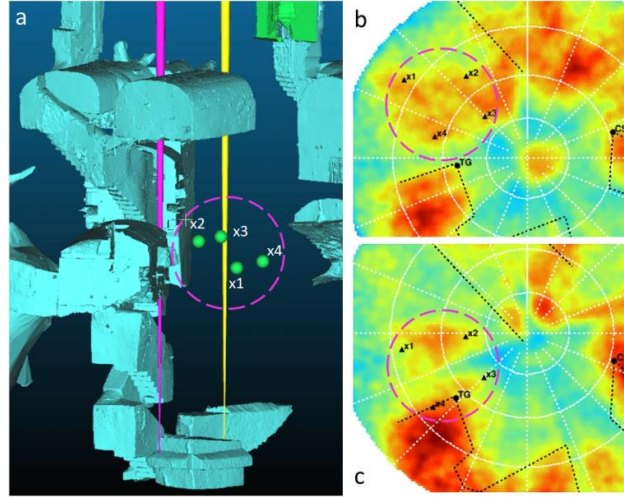
Muography uses cosmic muons to image the internal density structure of large objects.



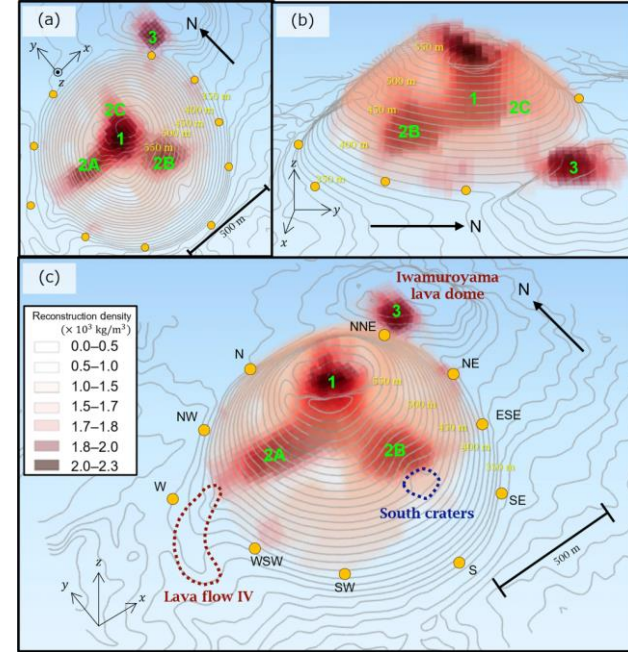
Cosmic rays<sup>2</sup>

# Muography application

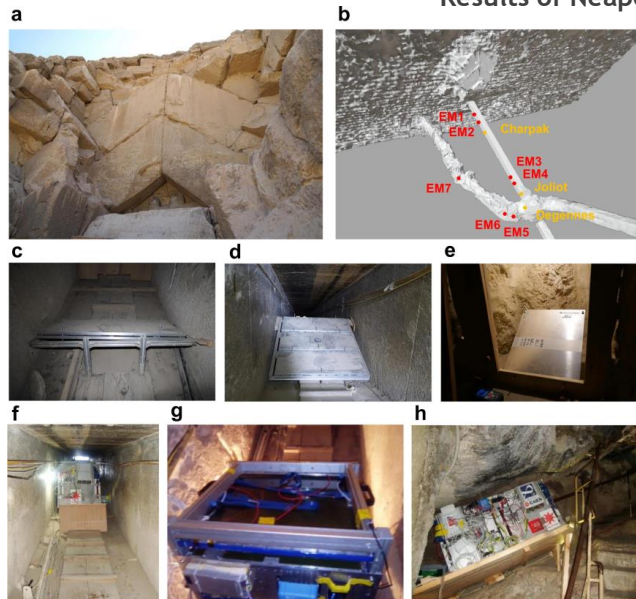
- ▶ **Vulcanology**
- ▶ **Speleology**
- ▶ **Mining**
- ▶ **Archaeology application**
- ▶ **Structural analysis**
- ▶ **Monitoring**



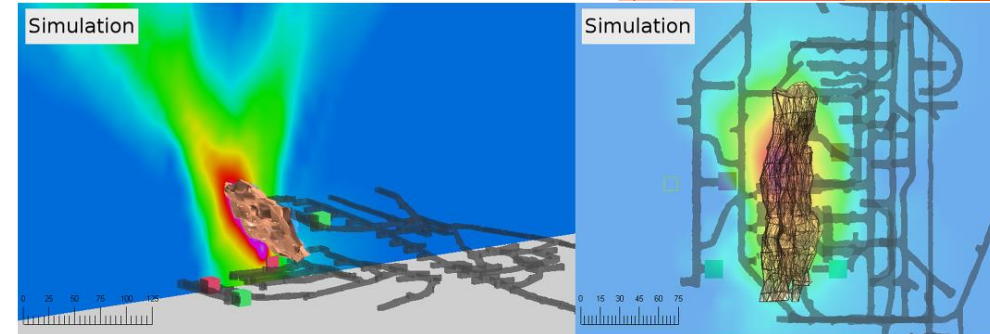
Results of Neapolis (Naples) measurements<sup>3</sup>



3D density tomography of Omuroyama scoria cone<sup>4</sup>



Archeology measurements in the Khufu's Pyramid<sup>5</sup>



Simulate data of uranium deposit<sup>6</sup>

# HUN-REN Wigner Group from Hungary

Country	Mining	Target
Finland	Kemi chromium mine	granite and ore bedrock localization (2.3-3.3g/cm <sup>3</sup> ; 2.65g/cm <sup>3</sup> )
Hungary	Janossy underground laboratory	test site, hidden inhomogeneities
Hungary	Királylaki tunnels	unknown caves, hidden inhomogeneities
Hungary	Esztramos mine	Well explores hill, unknown caves
Hungary	Underneath the Castle of Buda	expected medieval tunnels
Italy	Castello di Mussomeli	medieval tunnels
Japan	Sakurajima Muography Observatory	vulcanology



Underground measurement arrangement

```

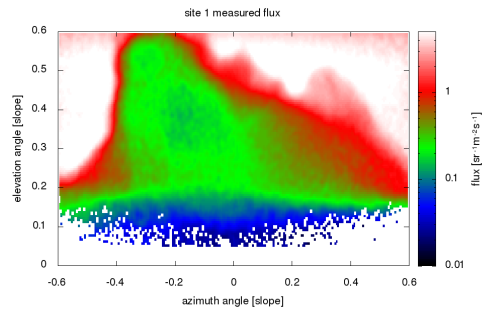
13
14 Load readout settings from file 'Default.rsin!' ...
15 From event 1 the ebe file is ../Measurements/Mts0_Run120.ebe (filename:0)
16 Event 0 , 2018-04-26_16:59:57 , dt : 3616236
17 .....XX.....XX.....
18 .....XX.....XX.....
19 .....X.....X.....
20 .....XX.....XX.....
21 .....XX.....XX.....
22 .....XX.....X.....
23 Adc : 2464 3202 3072 3584 3084 3447
24 THP : T= +19.75 oC, H= 40.0%, P= 968.0 mBar, ThpId: 0
25 Counter : +19 (19)
26 Pattern : Triggered on : 111111000000 (ok)
27
28

```

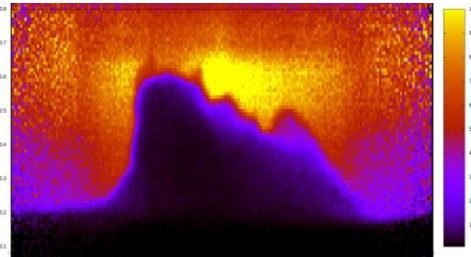
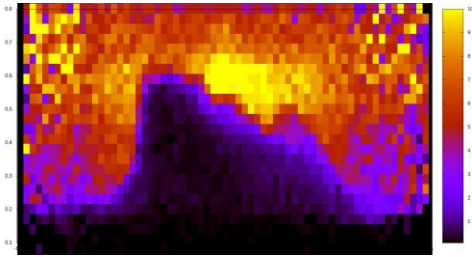
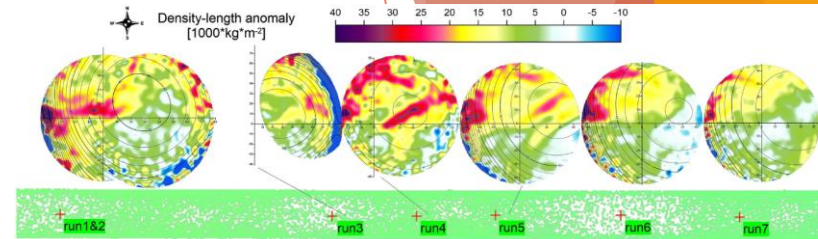
An event

A new research group has recently been set up, the High-Energy Geophysics Research Group.

# Muography Campaign Examples

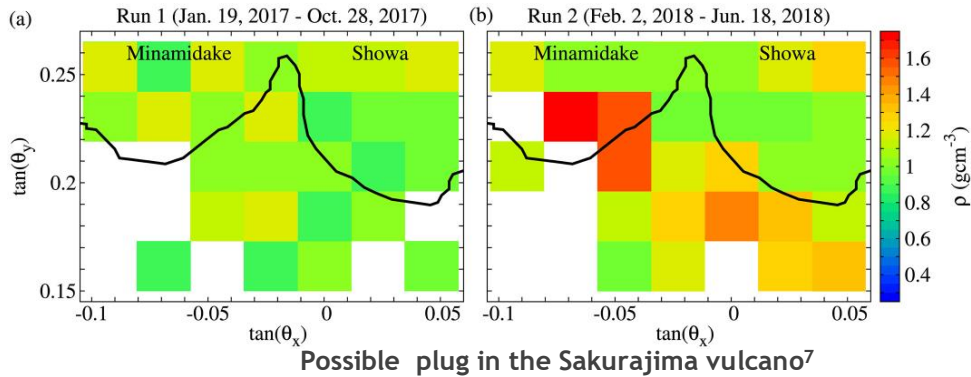
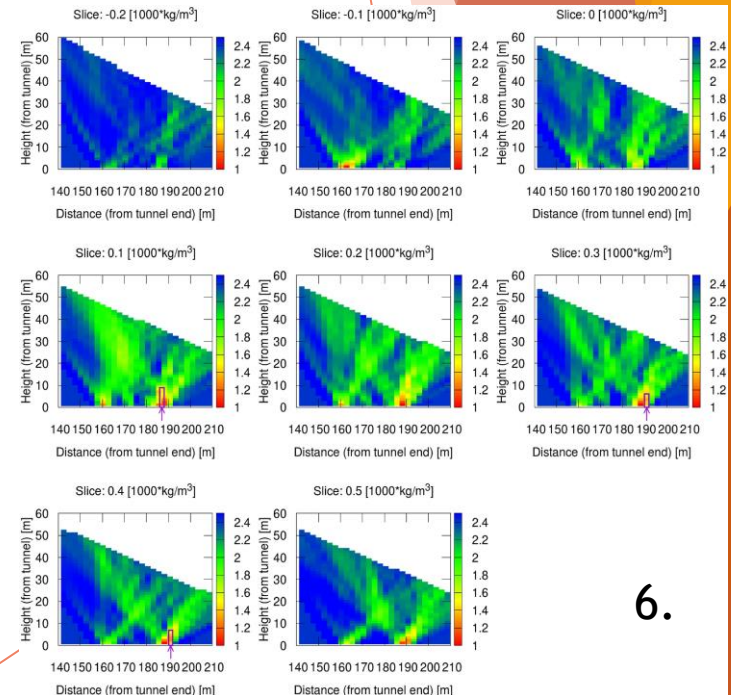


## Results of campaign of Királylaki tunnel<sup>8</sup>



Raw data of campaign of Mussomeli castle

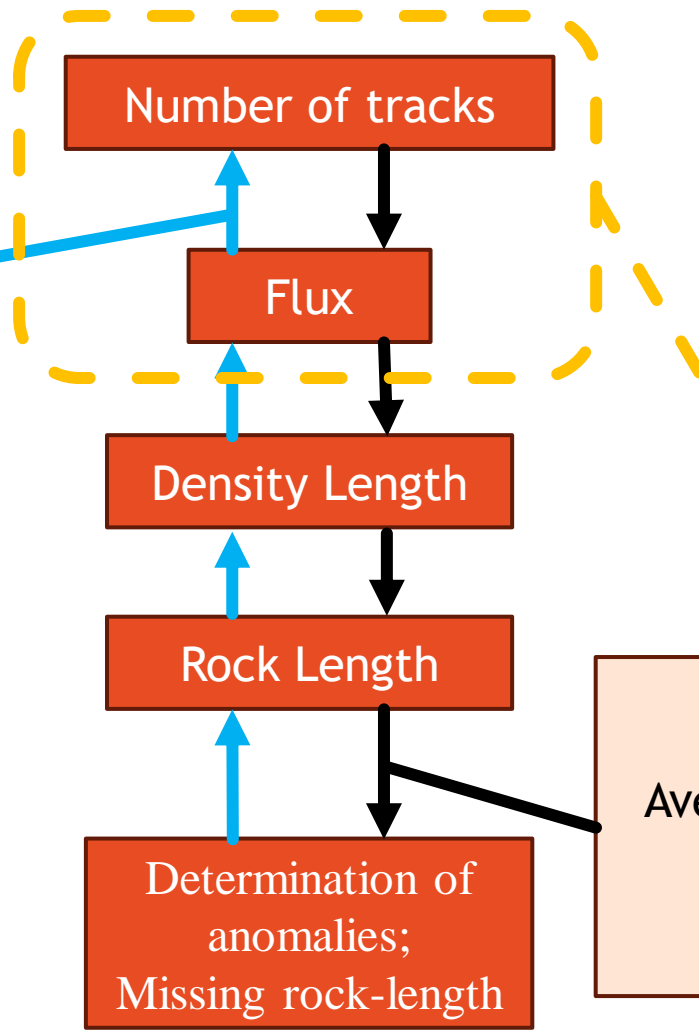
## Results slices of muotomographic inversion<sup>8</sup>



# Data processing

**Colors of arrows:**  
➤ Data processing  
➤ Measurement planning

Detector and measurement parameters (for unit time)



**Direct problem:**

- Detector effects
- Geometry
- Reconstruction algorithm

Average density-model / Surface geometry

Questions about planning:

- Detector type
- Detector position
- Measure time
- Sensitivity



# Direct problem models

$$N = Ft\Omega A_{\text{eff}}$$

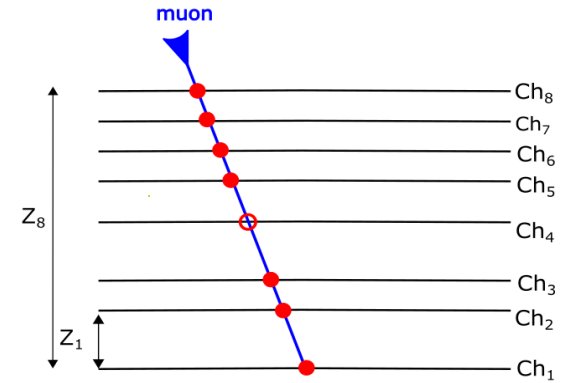
## Equidistant model

$$s_x = \tan(\alpha_x), \quad s_y = \tan(\alpha_y)$$

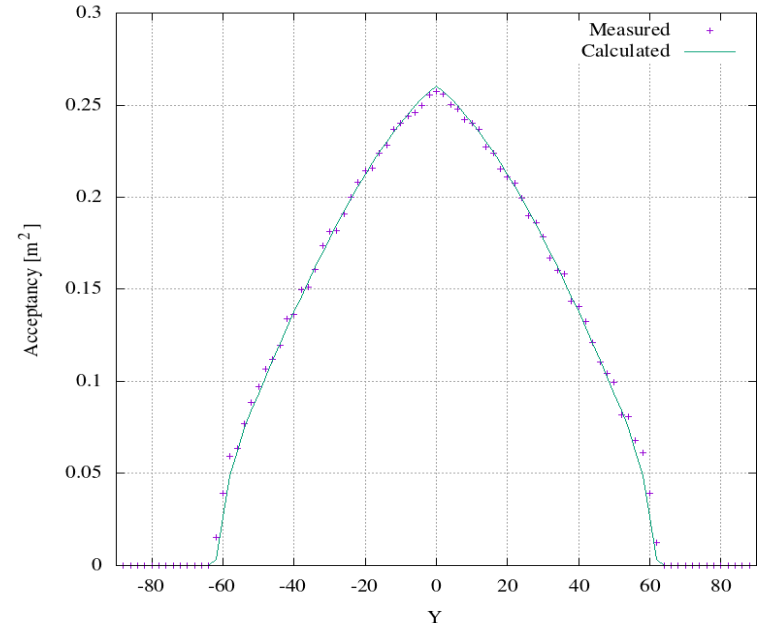
$$A_{\text{eff}} = \frac{(L_x - hs_x + 2(N_K - K)as_x)(L_y - hs_y + 2(N_K - K)as_y)}{\sqrt{1 + s_x^2 + s_y^2}} \eta$$

## Model for general detector geometry

$$A_{\text{eff}} = \int_{X_{11} + S_{x1}}^{X_{2N_K} + S_{xN_K}} \int_{Y_{11} + S_{y1}}^{Y_{2N_K} + S_{yN_K}} \eta(x, y) dy dx \frac{1}{\sqrt{1 + s_x^2 + s_y^2}}$$



Slices of models:  
Acceptancy (\$K\_T=6\$)

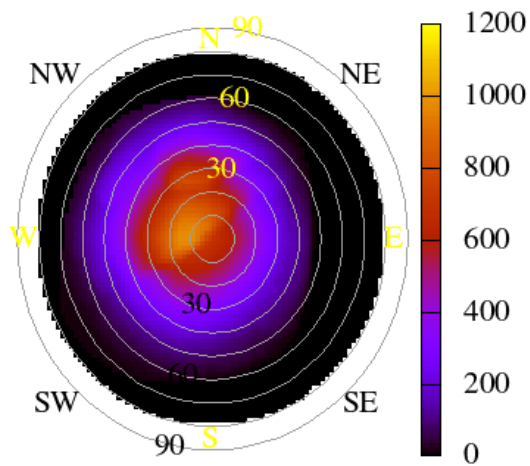


# Esztramos mine

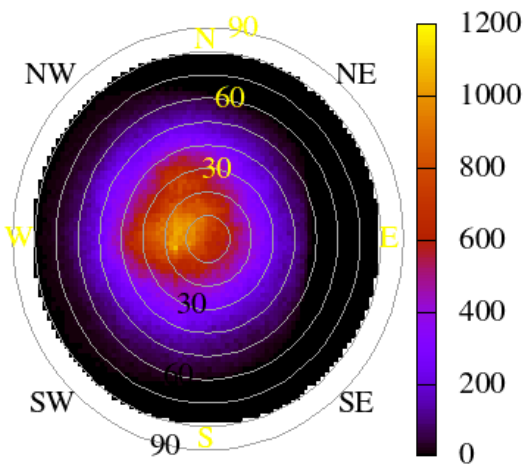
- ▶ **Goal: \* Model verification on real active underground measurement;**
- ▶ **\*quantitative assessment of the certainty of anomalies**
- ▶ No active mining in the mine = stable surface
- ▶ Active exploration in the mine
- ▶ A domestic measurement area

## Results of Esztramos mine

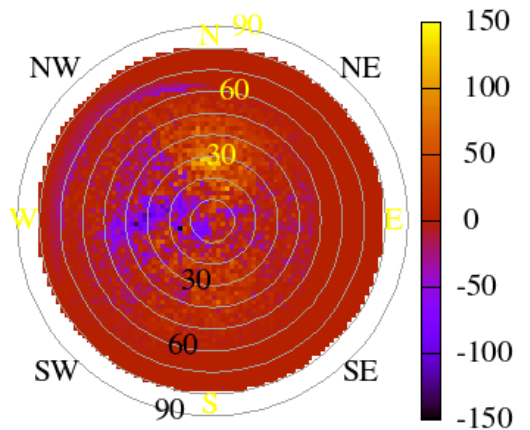
Number of Tracks calculated [1]



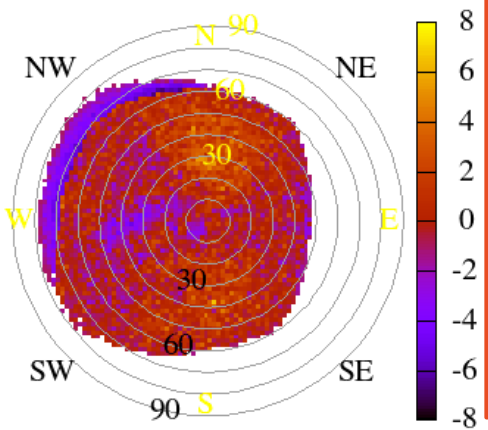
Number of Tracks measured [1]



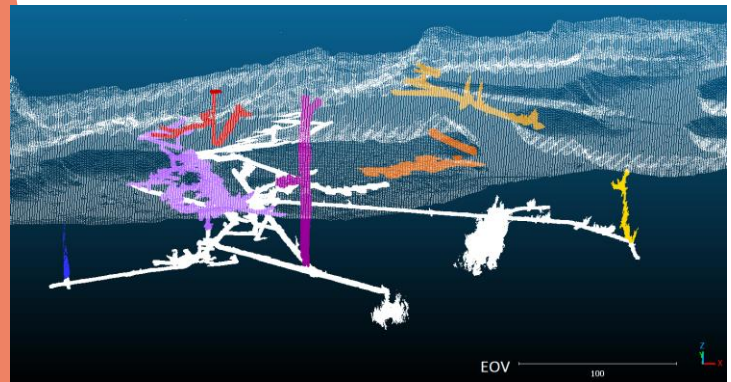
Number of Tracks difference (calculated-measured) [1]



Number of Tracks difference normalized with standard deviation [1]



$$\delta\sigma = (N_C - N_M) / \sqrt{N_M}$$



# Simple model : flat surface with an anomalous sphere

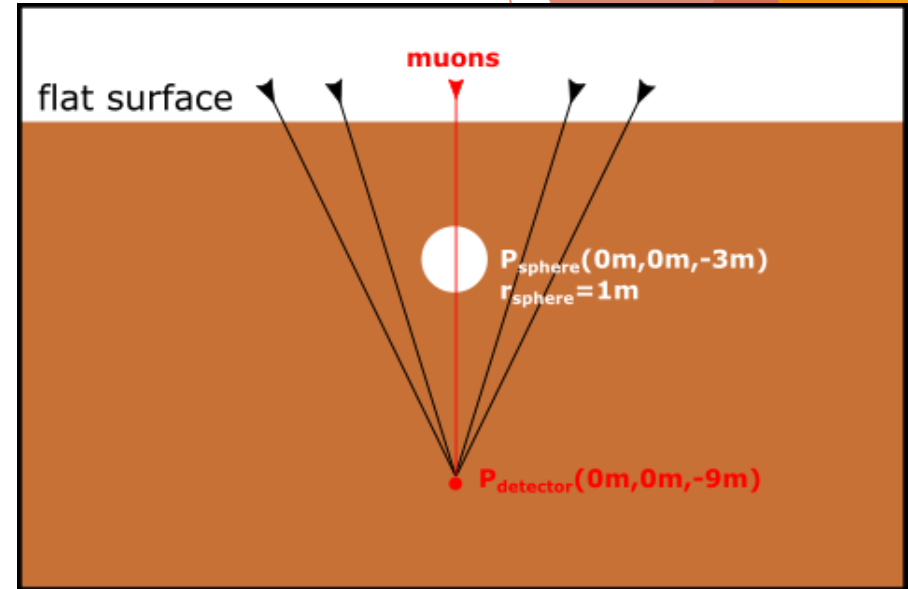
- ▶ **Goal: Presenting the measurement time estimation for a simple anomaly.**
- ▶ Different geology situations become possibly to search by this method
- ▶ We can review many questions with given series of measurement  
*e.g.:* What kind type of detector should we use in a measurement?

How long do we have to measure in a position?

Which setup can optimal ?

What type of anomaly can we detect?

- ▶ Ground model: flat surface, homogeneous,  $\rho_a = 2.4 \text{ g/cm}^3$
- ▶ Detector type= Mtl2, Position[0,0,-9]m, Inclination=0° and Rotation=0°
- ▶ Sphere: *Position [0,0,-3]m, Radius=1m,  $\rho_{sphere} = 1 \text{ g/cm}^3$  (water) and  $\rho_{sphere} = 0 \text{ g/cm}^3$  (air)*



# Simple model : flat surface with an anomalous sphere

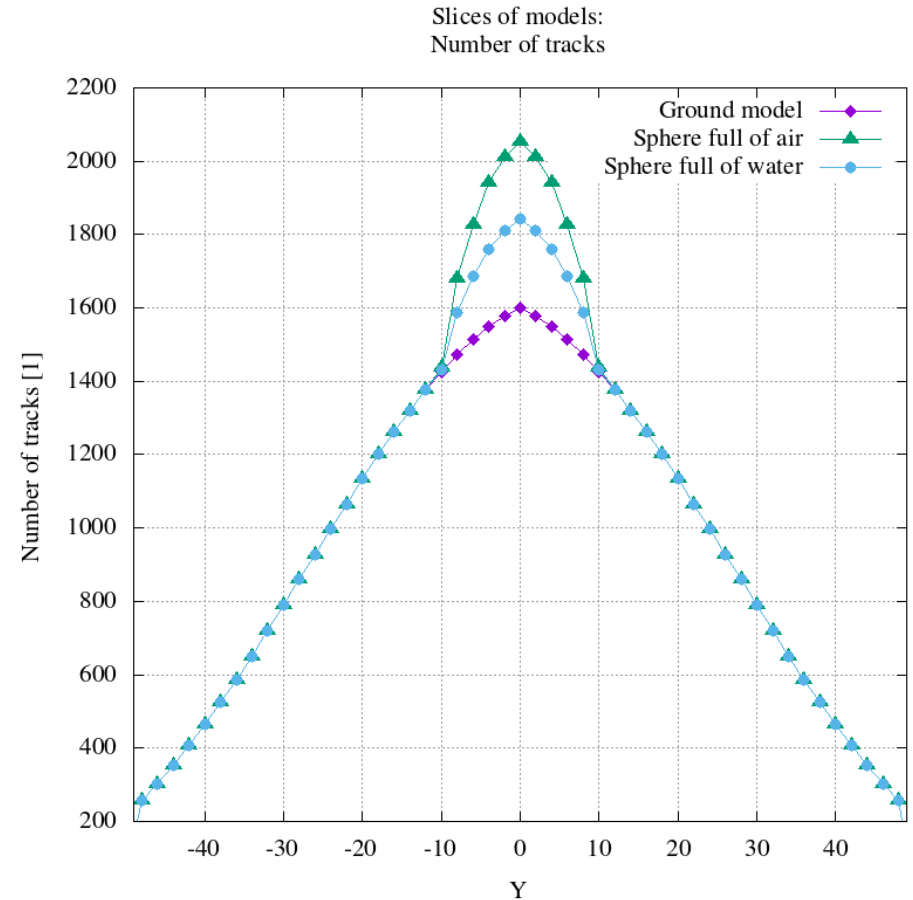
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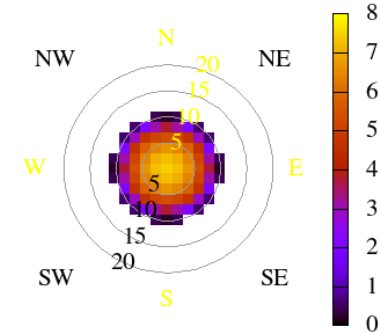
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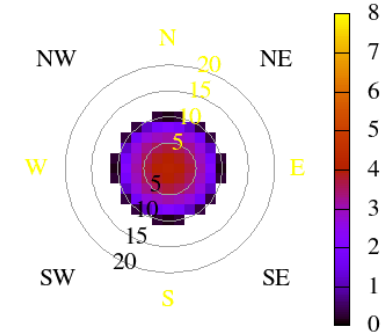
- ▶ Ground model: flat surface, homogeneous,  $\rho_a = 2.4 \text{ g/cm}^3$
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Results of sphere under the surface

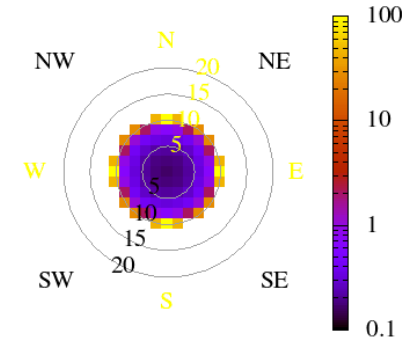
Sphere (air) under the surface:  
Sigma Difference [1/day]



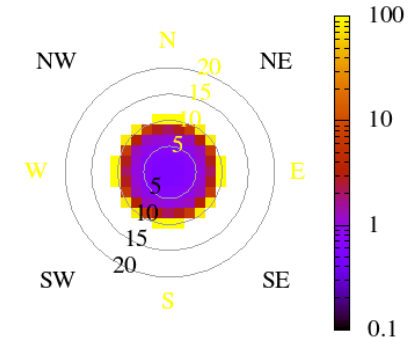
Sphere (water) under the surface:  
Sigma Difference [1/day]



Sphere (air) under the surface:  
Necessary measuretime [day]



Sphere (water) under the surface:  
Necessary measuretime [day]



# Test site: Janossy underground laboratory

► **Goal: Demonstration of time estimation for real underground measurements for known tunnels**

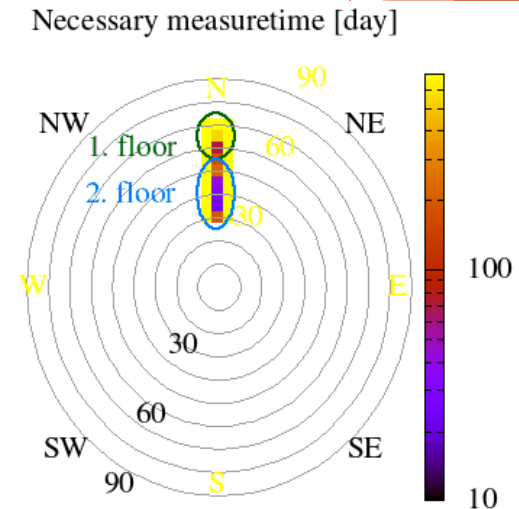
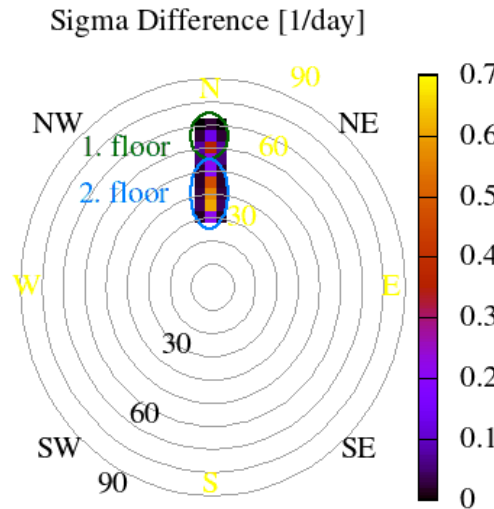
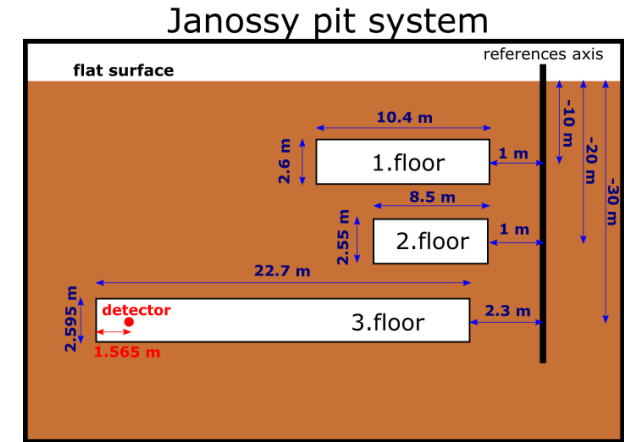
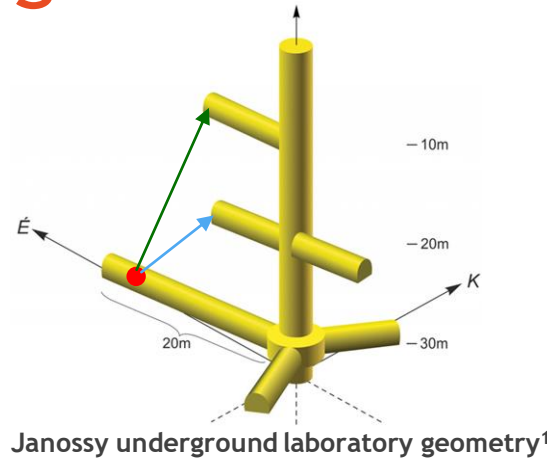
► Janossy underground laboratory : simple geometry (built for particle physics measurements 60 years ago)

- 3 floors:
1. 1 tunnel at -10 m ( $0^\circ$ )
  2. 2 tunnel at -20 m ( $0^\circ$ ,  $180^\circ$ )
  3. 3 tunnel at -30 m ( $0^\circ$ ,  $120^\circ$ ,  $240^\circ$ )

► Mts8 detector: position: 3. floor 1. tunnel, 156.5cm from the end of the tunnel; Inclination= $-45^\circ$ ; Rotation= $-90^\circ$

► Ground model: flat surface, (NOT jet the original surface); homogeneous  $\rho_a = 2.2 \text{ g/cm}^3$

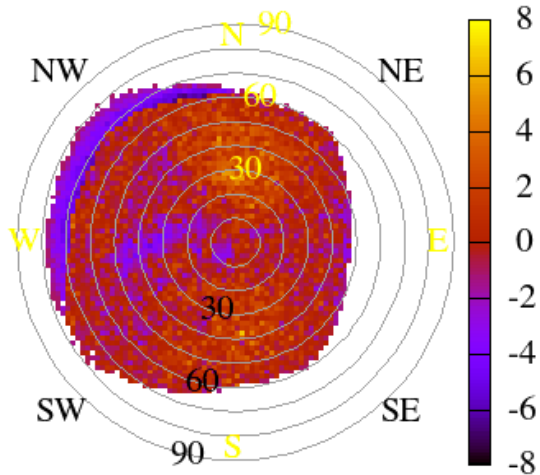
► Geology model: Shape of the tunnels were modelled as cylinders.  $\rho_{tunnels} = 0 \text{ g/cm}^3$



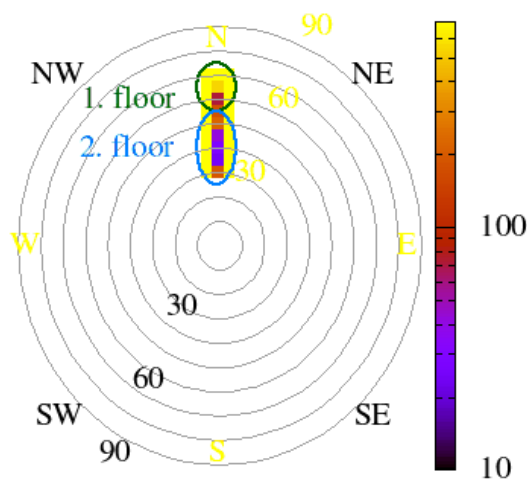
# Conclusion

- ▶ Muography uses cosmic muons to image the internal density structure of large objects.
- ▶ Muography applications: geophysics, mining, volcanology, speleology, Archaeology, Structural analysis, Monitoring application
- ▶ Precise model for Direct problem for general geometry -> Detector Optimization (type, position, inclination, rotation), Necessary Time estimation
- ▶ Model proved for : laboratory, underground, estimation demonstration

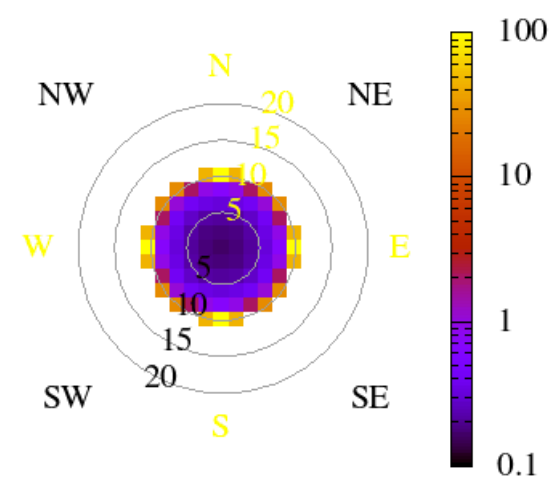
Number of Tracks difference  
normalized with standard deviation [1]



Necessary measuretime [day]



Sphere (air) under the surface:  
Necessary measuretime [day]



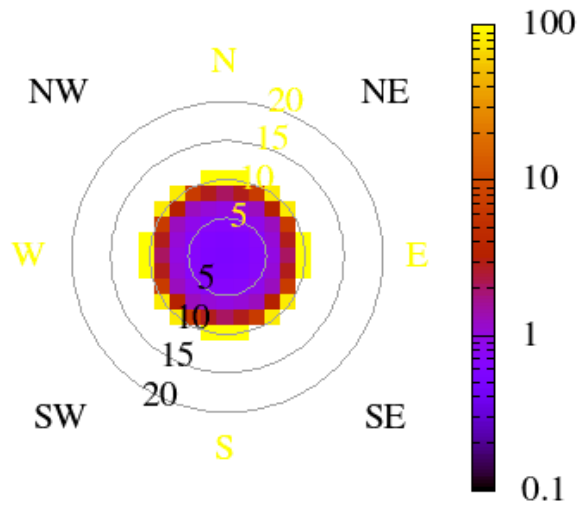
# Acknowledgement

▶ I would like to express my special thanks of gratitude to WignerRCP, REGARD Group, Gergő Hamar and László Balázs.

▶ This project is supported by:

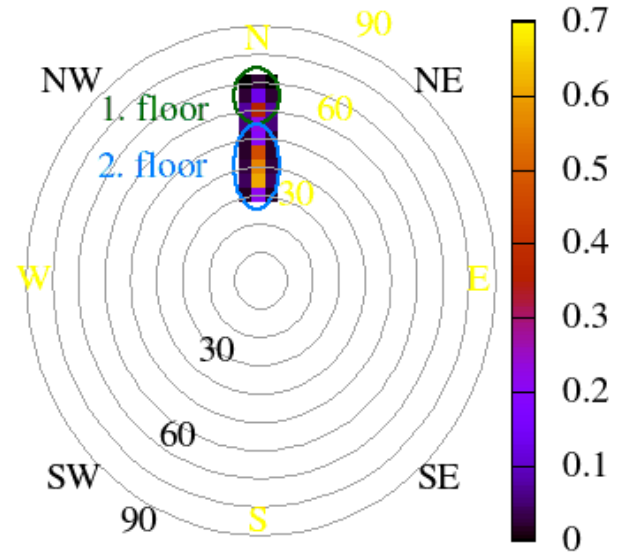
OTKA-FK135349, ELKH-KT-SA-88/2021, NKFIH-TKP2021-NKTA-10, KSZF-144/2023

Sphere (water) under the surface:  
Necessary measuretime [day]



Thank you for your attention!

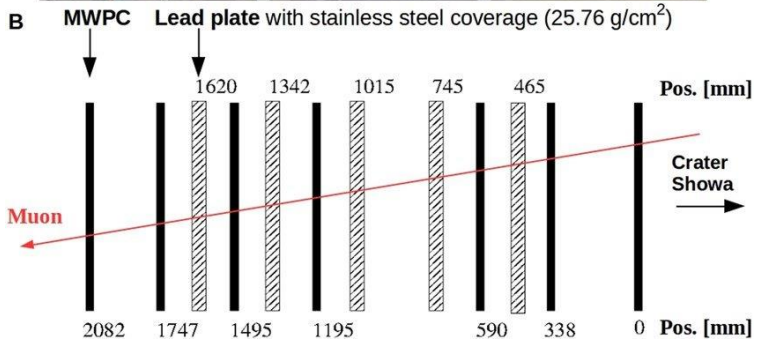
Sigma Difference [1/day]



# References

1. <https://rtl.hu/tudomany-tech/2023/08/18/janossy-lajos-kutato-labor-akna-foldalatti>
2. <https://home.cern/science/physics/cosmic-rays-particles-outer-space>
3. <https://www.nature.com/articles/s41598-023-32626-0?fromPaywallRec=true>
4. <https://link.springer.com/article/10.1007/s00445-022-01596-y/figures/9>
5. <https://www.nature.com/articles/s41467-023-36351-0>
6. <https://agupubs.onlinelibrary.wiley.com/doi/full/10.1029/2018JB015626>
7. <https://agupubs.onlinelibrary.wiley.com/doi/full/10.1029/2019GL084784>
8. <https://academic.oup.com/gji/article/236/1/700/7335291>

Back up slides

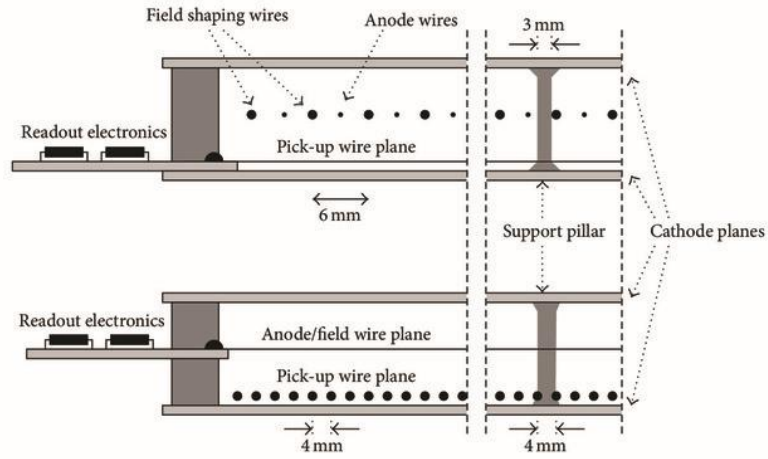


Surface measurement arrangement

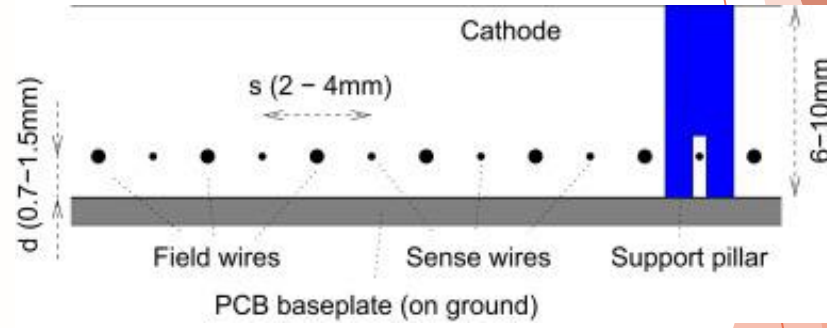


Borehole measurement arrangement

# Detector types



MWPC



CCC

# Direct problem models

$$N = Ft\Omega A_{\text{eff}}$$

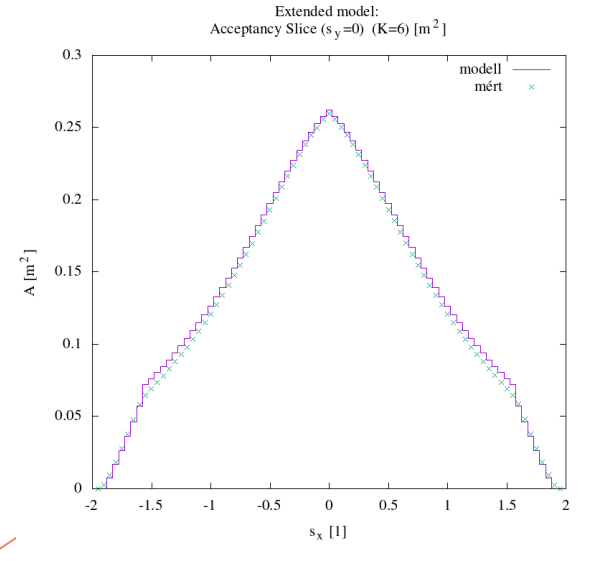
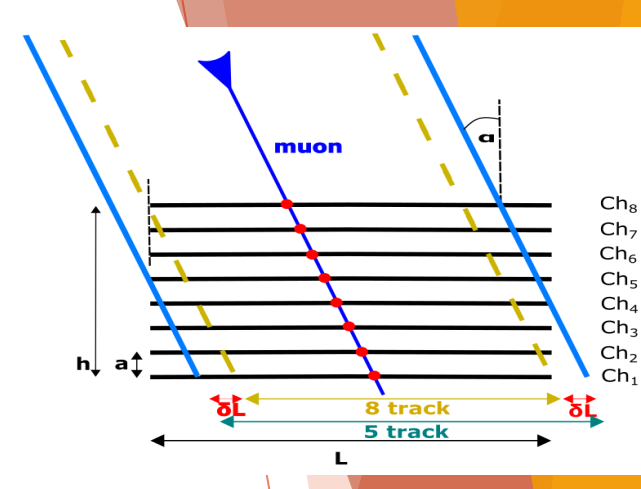
## Extended equidistant model in 1D

Slice:  $s_y = 0$

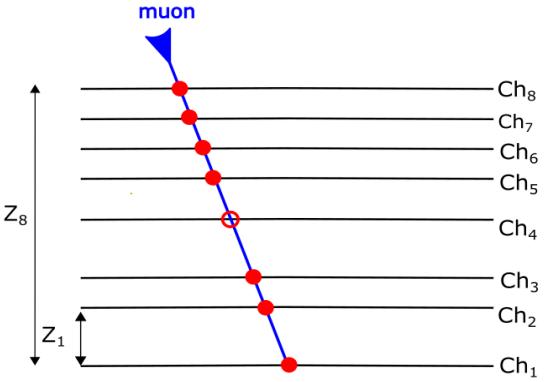
$$l_x(s_x) = \begin{cases} L - h|s_x| + 2(N_K - K)a|s_x|, & |s_x| < L/h \\ (L - (K - 1)a|s_x|) + (N_K - K)a|s_x|, & L/h < |s_x| < L/(Ka) \\ (N_K - (K - 1))(L - (K - 1)a|s_x|), & L/(Ka) < |s_x| < L/((K - 1)a) \\ 0, & |s_x| > L/((K - 1)a) \end{cases}$$

$$\eta(K_T) = \begin{cases} 1, & K_T > K \\ \eta_{\text{Chamber}}^K, & K_T == K \\ 0, & \end{cases}$$

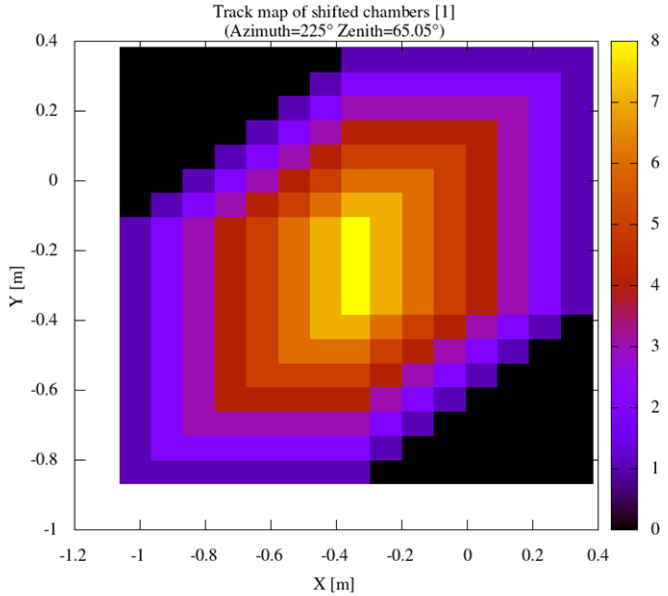
$$A_{\text{eff}} = l_x L_y \frac{1}{\sqrt{1+s_x^2}} \eta$$



# Direct problem model for general detector geometry



- ▶ Different approach was used
- ▶ What happens the chamber position from the perspective of incoming muons? → Shifted
- ▶ So I can calculate how many chambers the muon has passed in a given area through
- ▶ The intersection of the chambers in 2D = how many chambers detected the given angle of the muons in the intersection area



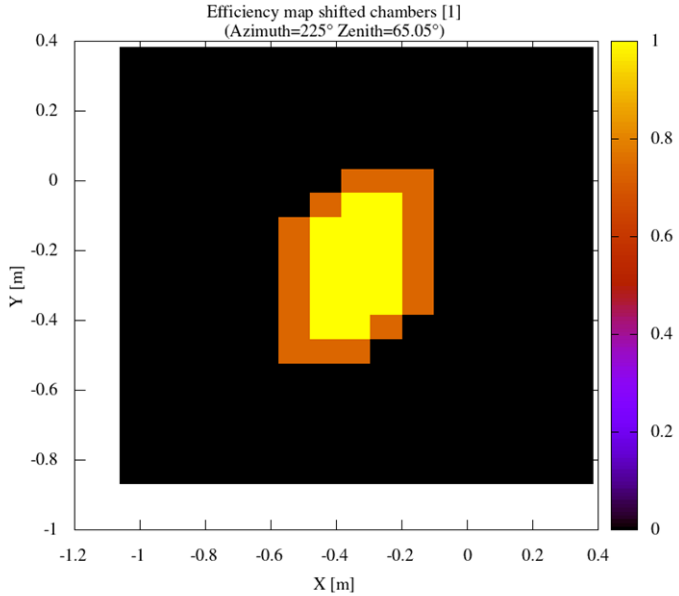
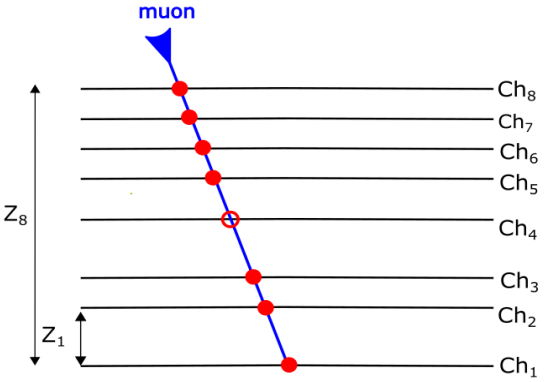
$$K_T(x, y) = \sum_i^{N_K} \begin{cases} 1, & (X_{1i} + S_{x_i}) \leq x \leq (X_{2i} + S_{x_i}) \text{ és } (Y_{1i} + S_{y_i}) \leq y \leq (Y_{2i} + S_{y_i}) \\ 0 \end{cases}$$

$$S_{x_i} = Z_i s_x, \quad S_{y_i} = Z_i s_y, \quad i = 1, \dots, N_K$$

$$\eta(x, y) = \begin{cases} 1, & K_T > K \\ \eta_{Chamber}^K, & K_T == K \\ 0 \end{cases}$$

$$A_{eff} = \int_{X_{11} + S_{x_1}}^{X_{2N_K} + S_{x_{N_K}}} \int_{Y_{11} + S_{y_1}}^{Y_{2N_K} + S_{y_{N_K}}} \eta(x, y) dy dx \frac{1}{\sqrt{1 + s_x^2 + s_y^2}}$$

# Direct problem model for general detector geometry



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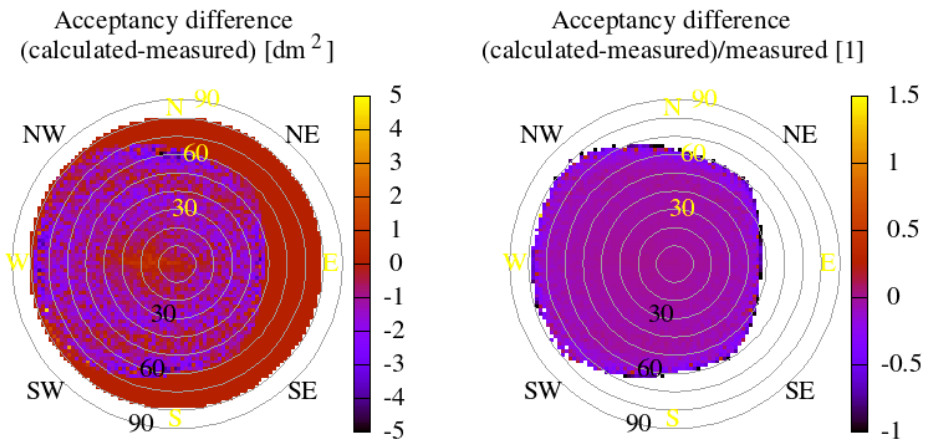
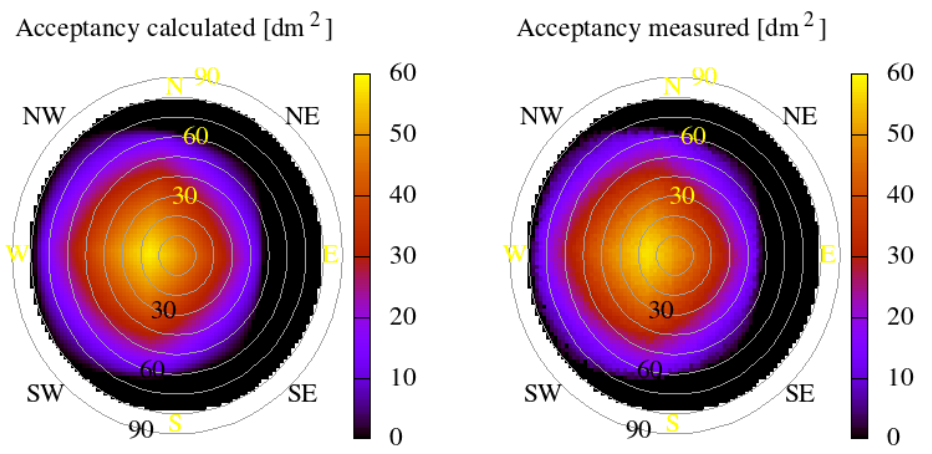
$$S_{x_i} = Z_i s_x, \quad S_{y_i} = Z_i s_y, \quad i = 1, \dots, N_K$$

$$\eta(x, y) = \begin{cases} 1, & K_T > K \\ \eta_{Chamber}^K, & K_T == K \\ 0 \end{cases}$$

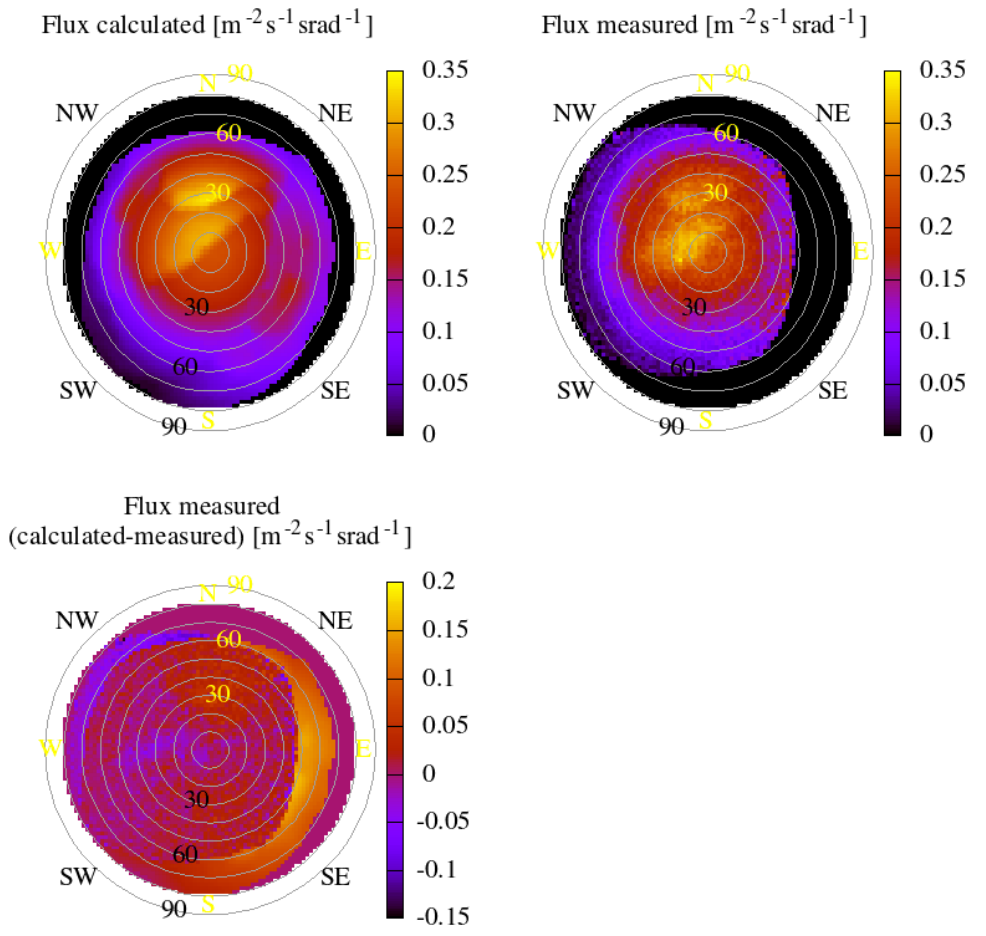
$$A_{eff} = \int_{X_{1_1} + S_{x_1}}^{X_{2_{N_K}} + S_{x_{N_K}}} \int_{Y_{1_1} + S_{y_1}}^{Y_{2_{N_K}} + S_{y_{N_K}}} \eta(x, y) dy dx \frac{1}{\sqrt{1 + s_x^2 + s_y^2}}$$

# Esztramos mine

Acceptancy results of Esztramos mine



Flux results of Esztramos mine

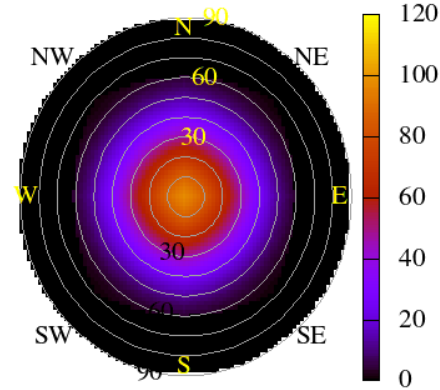


# Simple geology model: flat surface with half sphere anomaly on the surface

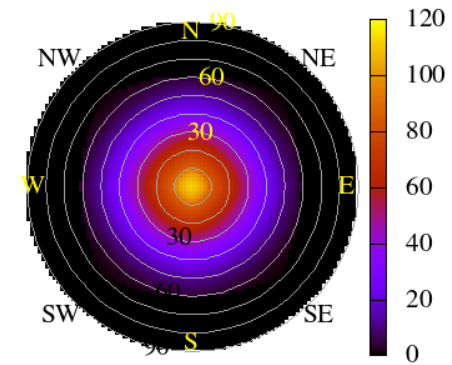
- ▶ Ground model: flat surface, homogeneous,  $\rho_a = 2.4 \text{ g/cm}^3$
- ▶ Anomaly:
  - half ball on the surface
  - (Position[0,0,0]m, r=1m)
  - Dector type=Mtl2 ,
  - Position[0,0,-6]m, Inc=0° and Rot=0°

Results of half sphere on the surface

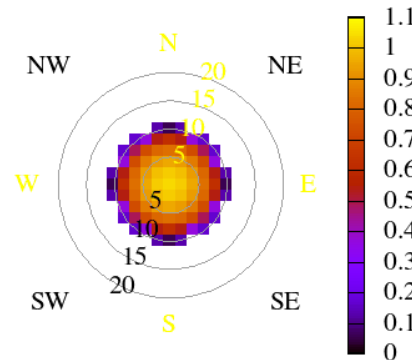
Flat Surface: Number of tracks [1]



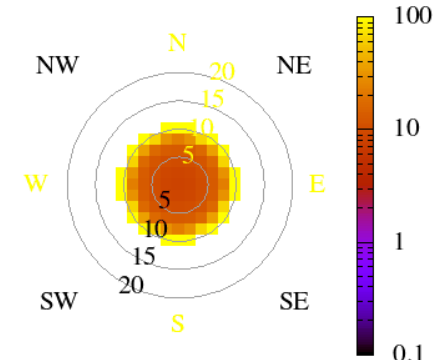
Negative half sphere on the surface: Number of tracks [1]



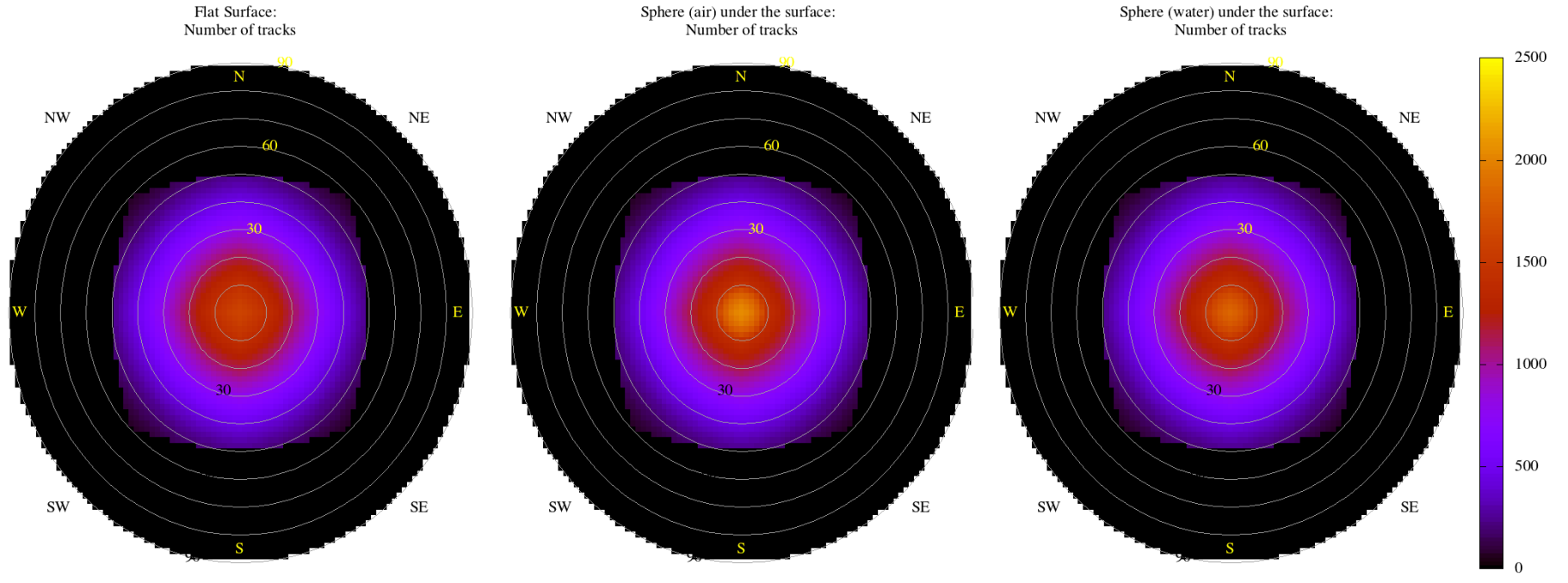
Negative half sphere on the surface: Sigma Difference [1/hour]



Negative half sphere on the surface: Necessary measuretime [hour]

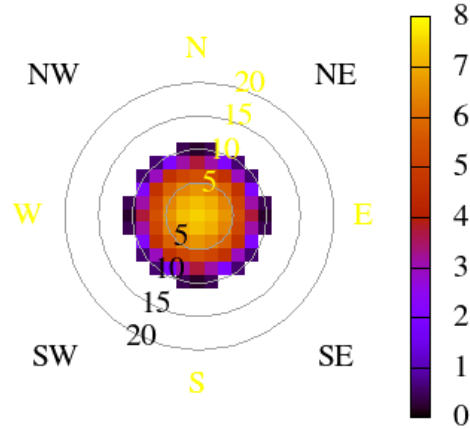


# Simple model : flat surface with an anomalous sphere

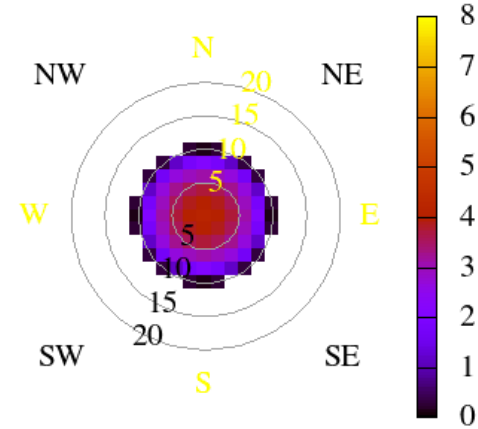


Results of sphere under the surface

Sphere (air) under the surface:  
Sigma Difference [1/day]

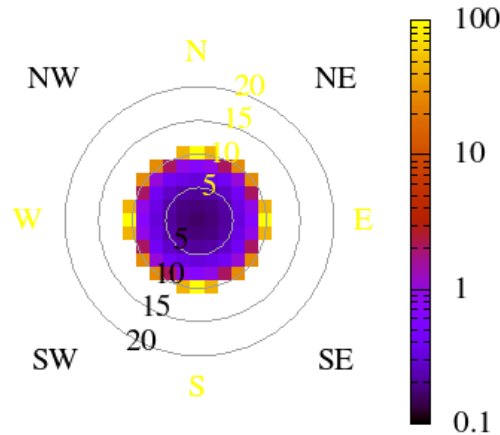


Sphere (water) under the surface:  
Sigma Difference [1/day]

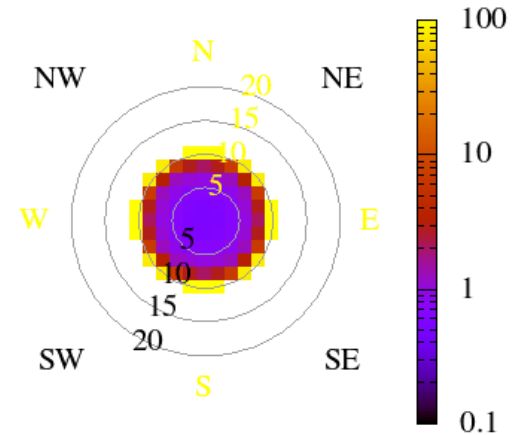


$$\delta\sigma = (N_C - N_M) / \sqrt{N_M + N_C}$$

Sphere (air) under the surface:  
Necessary measurementtime [day]



Sphere (water) under the surface:  
Necessary measurementtime [day]

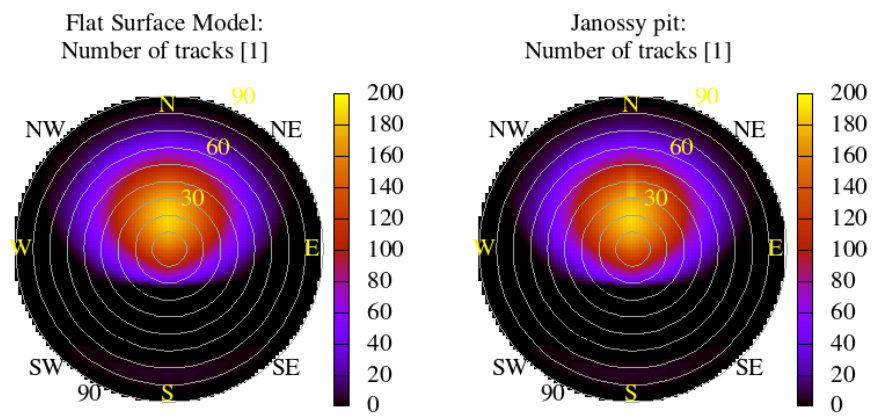


$$\sigma_{separation} = 3$$

$$t = \sigma_{separation} / \delta\sigma$$

# Janossy underground laboratory

Results of Janossy pit system



Results of Janossy pit system

